

GPS trajectory imputation: A hybrid approach combined clustering and GAIN-based algorithm

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ABSTRACT

The advancement of computing power and the proliferation of big data have opened unprecedented avenues for the Intelligent Transportation Systems (ITS) community to extract valuable insights from Global Positioning System (GPS) trajectory data. However, the reality of real-world GPS trajectory data often lacks complete information due to various factors (e.g. detector damage, transmission loss, ...), thus posing significant challenges for trajectory analysis and operational efficiencies within transportation systems. To address this issue, time series data imputation techniques have emerged as critical solutions to accurately fill in missing data points. Existing imputation approaches can be classified into statistical methods and deep generative models. Significantly, within the domain of deep generative models, Generative Adversarial Imputation Networks (GAIN) have exhibited promise in the realm of data imputation. Nonetheless, their limited capacity to effectively handle time series data represents a notable limitation. Additionally, GPS trajectories, particularly those of buses, exhibit a distinctive characteristic wherein each vehicle is assigned to one or more predetermined routes, adding complexity to the data imputation process. In response to these challenges, this study proposes a novel hybrid imputation approach, Cluster-GRUI-GAIN, which integrates clustering techniques (e.g. KNN) with the enhanced generative adversarial imputation network, GRUI-GAIN. By combining the strengths of clustering and GAIN, our hybrid approach aims to enhance the accuracy of time series data imputation for GPS trajectories with diverse missing rates and significant gaps. Specifically, the GRUI-GAIN model within our proposed Cluster-GRUI-GAIN framework incorporates GRUI (GRU for Imputation) within the generator. This strategic integration enhances the model's ability to effectively handle missing data within time series, thereby bolstering the accuracy and reliability of imputations. Experimental evaluations on real-world dataset demonstrate that our proposed Cluster-GRUI-GAIN approach outperforms baseline methods in terms of time series imputation accuracy and offers robust and accurate imputations, making it well-suited for practical transportation applications.

Key words: GPS trajectory, data imputation, generative adversarial network, clustering, hybrid

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1 INTRODUCTION

2 With the exponential growth of computing power
3 and the abundance of big data, the Intelligent Transportation Systems (ITS) community now has an unprecedented opportunity to extract valuable insights
4 from the vast amount of data available. GPS trajectory data which is time series data plays a crucial role in numerous applications and research endeavors within transportation systems. Whether it is facilitating route planning for individuals or aiding transportation management and control for researchers and governments, the availability of comprehensive GPS trajectory data is essential¹. Unfortunately, actual GPS trajectory data obtained from sensors or other sources often suffer from incomplete information due to various factors. Numerous studies
5 have highlighted the issue of missing data in various trajectory and transportation databases. For instance,

Qu et al.² identified missing data ratios in Beijing typically around 10%, but occasionally reaching as high as 20% to 25% due to various factors. These data gaps pose significant challenges for trajectory analysis and other practical operations.

To address this issue, trajectory data imputation or more generally, time series data imputation emerges as a critical technique aimed at accurately filling in these missing data points. Given the ever-increasing richness of traffic data, trajectory data imputation remains a pressing and highly relevant area of investigation³.

Existing techniques for handling missing data can be broadly classified into two main categories: statistical methods and deep generative models. Statistical approaches frequently rely on stringent assumptions concerning the nature of missing data patterns. For example, mean/median averaging⁴, linear regression⁵, MICE⁶, and K-nearest neighbors⁷ can only

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38 handle data missing at random. Latent variables mod-
 39 els with EM algorithm⁸ can impute data missing not
 40 at random but are restricted to certain parametric
 41 models. The deep generative models offer a flexible
 42 framework for missing data imputation. For instance,
 43 several studies^{9–11} develop variants of recurrent neu-
 44 ral networks to impute time series. Luo et al.¹² lever-
 45 age generative adversarial training (GANs)¹³ to learn
 46 complex missing patterns.

47 Notably, Yoon et al.¹⁴ introduced the Generative Ad-
 48 versarial Imputation Network (GAIN), a pioneer-
 49 ing approach for addressing missing data imputation.
 50 This method has significantly propelled the field of
 51 data imputation by employing a generator that pro-
 52 duces a completed vector based on the available ob-
 53 servations, while a discriminator endeavors to dis-
 54 cern between the entries in the completed dataset that
 55 originated from observations and those that were im-
 56 puted. Nonetheless, a noteworthy limitation of GAIN
 57 lies in its relatively diminished capacity to effectively
 58 impute missing data within time series datasets.

59 Moreover, GPS trajectories, particularly GPS bus tra-
 60 jectories, possess the distinctive characteristic of each
 61 vehicle being assigned to one or more predetermined
 62 routes. Alabadla et al.¹⁵ highlight the effectiveness
 63 of hybrid approaches that combine multiple machine
 64 learning methods, resulting in improved imputation
 65 performance. Building upon this insight, we pro-
 66 pose a hybrid approach in this study that integrates
 67 clustering techniques with the enhanced generative
 68 adversarial imputation network (GRUI-GAIN). Our
 69 aim is to enhance the accuracy of GAIN when deal-
 70 ing with diverse missing rates and significant miss-
 71 ing gaps in the GPS trajectory data. By leveraging the
 72 strengths of both clustering and GAIN-based, we an-
 73 ticipate achieving more accurate and robust imputa-
 74 tions in scenarios where missing data is prevalent. In
 75 particular, we make the following technical contribu-
 76 tions:

- 77 • We propose a hybrid approach called Cluster-
 78 GRUI-GAIN to improve the GPS trajectory im-
 79 putation accuracy of clustering and GAIN un-
 80 der various missing values and large missing
 81 gaps by combining these two methods.
- 82 • We utilize the GAIN-based model, which in-
 83 corporates GRUI (GRU for Imputation) within
 84 the generator, enhancing its ability to handle
 85 missing data in time series, thereby enhancing
 86 the imputation quality of GAIN¹⁴ in time se-
 87 ries. We refer to this improved model as GRUI-
 88 GAIN.

- We evaluate our model on real-world datasets. 89
 Experimental results show that our model out- 90
 performs the baselines in terms of the accuracy 91
 of time series imputation. 92

RELATED WORKS

A. Generative Adversarial Networks

93
 94
 95 Neural networks have significant advancements and
 96 have been widely employed across various practi-
 97 cal applications. Numerous neural network models
 98 have been proposed to tackle different problem do-
 99 mains^{16,17}. Notably, generative adversarial network
 100 (GANs)¹³, a framework for constructing generative
 101 models approximating the target distribution, has
 102 emerged as a powerful approach and achieved state-
 103 of-the-art performance in diverse learning tasks^{18–20}.
 104 GANs are characterized by their discriminator, which
 105 plays a pivotal role in discerning the discrepancy be-
 106 tween the generated distribution and the target dis-
 107 tribution. The GANs algorithm follows an iterative
 108 training process, where the discriminator progres-
 109 sively provides a more rigorous critique of the gen-
 110 erator’s outputs. This interplay between the genera-
 111 tor and discriminator leads to the refinement and im-
 112 provement of the overall model performance. GANs
 113 have proven to be highly effective in capturing com-
 114 plex data distributions, enabling the generation of re-
 115 alistic samples, and enhancing the quality of gener-
 116 ated outputs in various domains.

B. Deep Generative Imputation Methods

117
 118 Several imputation methods utilizing GAN frame-
 119 works have been introduced in the literature. Luo et
 120 al.¹² propose GRUI (GRU for Imputation), which ef-
 121 fectively models the temporal information of incom-
 122 plete time series data. In their GAN model, both the
 123 generator and discriminator are based on the GRUI
 124 architecture. Building upon this work, Luo et al.²¹
 125 present E2GAN, an end-to-end imputation method
 126 that offers improvements over the previous two-stage
 127 approach in¹². E2GAN employs an auto-encoder
 128 based on GRUI as its generator, aiming to simplify
 129 model training difficulties and enhance imputation
 130 performance.

131 Moreover, in the realm of missing value imputation
 132 for multivariate time series data, Miao, Xiaoye, et al²²
 133 introduce SSGAN, a novel semi-supervised genera-
 134 tive adversarial network model, with a generator, dis-
 135 criminator, and classifier. By incorporating a tempo-
 136 ral reminder matrix and a semi-supervised classifier,
 137 SSGAN achieves remarkable improvements in impu-
 138 tation and prediction performance when compared to

139 existing methods, as demonstrated through extensive
 140 experiments on benchmark time series datasets.
 141 In addition, Liu et al.²³ propose a non-autoregressive
 142 model named NAOMI for spatiotemporal sequence
 143 imputation. NAOMI comprises a bidirectional en-
 144 coder and a multiresolution decoder, which work to-
 145 gether to effectively handle missing data in spatiotem-
 146 poral sequences. Adversarial training techniques are
 147 further incorporated to enhance the imputation per-
 148 formance of NAOMI.
 149 These advancements in GAN-based imputation
 150 methods, such as GRUI, E2GAN, NAOMI, and
 151 SSGAN demonstrate the ongoing efforts to address
 152 the challenges of incomplete time series and spa-
 153 tiotemporal data imputation, leading to improved
 154 imputation performance in diverse domains.

155 **C. Clustering-based Imputation**

156 Clustering is a data partitioning technique that in-
 157 volves grouping a dataset into distinct classes or clus-
 158 ters based on specific criteria, such as a distance met-
 159 ric. The primary objective of clustering is to max-
 160 imize the similarity among data objects within the
 161 same cluster while ensuring significant differences be-
 162 tween objects belonging to different clusters.
 163 Clustering finds applications in diverse fields, includ-
 164 ing data compression, information retrieval, pattern
 165 recognition, and bioinformatics. It also holds the po-
 166 tential for imputing missing data sets. In the context
 167 of imputation, clustering can be approached in two
 168 ways. One approach involves dividing the original
 169 dataset into complete and missing subsets. The com-
 170 plete dataset is then clustered to obtain distinct clus-
 171 ters. Subsequently, missing data objects are assigned
 172 to the most similar clusters based on a similarity mea-
 173 surement, and the information within the clusters is
 174 utilized to fill in the missing values. The other ap-
 175 proach involves initializing the original dataset and
 176 directly clustering it, potentially redefining the sim-
 177 ilarity measure.
 178 In recent developments, clustering – based ap-
 179 proaches have begun incorporating temporal, spatial,
 180 global, and local perspectives. For example, Xiuwen
 181 et al.²⁴ employed a multi-view learning method based
 182 on temporal and spatial correlations to impute time
 183 series data. The primary objective of clustering tech-
 184 niques is to classify datasets into clusters by minimiz-
 185 ing intra-cluster dissimilarity, thereby enabling effec-
 186 tive data organization and analysis.

187 **PROBLEM FORMULATION**

188 In the context of GPS trajectory data, as depicted in
 189 Table 1, a fundamental format consists of timestamp,

latitude, and longitude coordinates. Timestamps pro-
 vide temporal context, indicating when the location
 was recorded, while latitude and longitude specify the
 vehicle’s geographic position.

Let X represent the GPS trajectory data which can also
 be interpreted as time series data in a d -dimensional
 space and observed over n timestamps $T = \{t_0, t_1, \dots, t_{n-1}\}$,
 is represented as: $X = \{x_0, x_1, \dots, x_{n-1}\} \in \mathbb{R}^{n \times d}$,
 where x_i is the i -th observation vector within X , and
 x_{ij} represents the j -th feature within the observation
 vector x_i .

In this study, the dimensionality, d , is set to 2, repre-
 senting the two geographic coordinates (latitude and
 longitude). We refer to X as the data vector and also
 define the mask matrix, denoted as M , which serves
 the purpose of indicating which components of X are
 missing, and it is defined as follow:

$$m_{ij} = \begin{cases} 0, & \text{if } x_{ij} \text{ is not observed} \\ 1, & \text{otherwise} \end{cases}$$

We define a matrix $\delta \in \mathbb{R}^{n \times d}$ that records the time gap
 from the last observation to the current timestamp,

$$\delta_{ij} = \begin{cases} t_i - t_{i-1}, & \text{if } m_{(i-1)j} = 1, i > 0 \\ \delta_{ij} + t_i - t_{i-1}, & \text{if } m_{(i-1)j} = 0, i > 0 \\ 0, & \text{if } i = 0 \end{cases}$$

209 **METHOD: IMPUTATION BASED ON GAIN**

211 **A. Trajectory Part Clustering**

212 The core idea of the hybrid imputation approach is to
 213 use the clustering technique to generate a small rep-
 214 resentative training dataset, which is applied to impu-
 215 tation in the GRUI-GAIN model. Figure 1 shows the
 216 whole framework of the proposed hybrid approach.
 217 Firstly, we divide the imputation into coarse and
 218 fine imputation. The original dataset is first imputed
 219 with the Last Observation Carried Forward (LOCF)²⁵
 220 method. This step prevents the clustering algorithm
 221 from dealing with the missing dataset directly. Sub-
 222 sequently, the dataset X' is clustered using the K-
 223 Means clustering algorithm to generate different clus-
 224 tering results $\{X'_1, X'_2, \dots, X'_n\}$. Finally, each cluster is
 225 finely imputed by using GRUI-GAIN. The structure
 226 of GRUI-GAIN model is shown at Figure 3. The new
 227 complete dataset Y is obtained by merging the clus-
 228 ters.

Table 1: Sample of GPS Trajectory Data.

Timestamp	Latitude	Longitude
2019-07-01 17:03:53	23.49468633	87.31687190
2019-07-01 17:03:54	23.49459298	87.31687570
2019-07-01 17:03:55	23.49455566	87.31686814
...

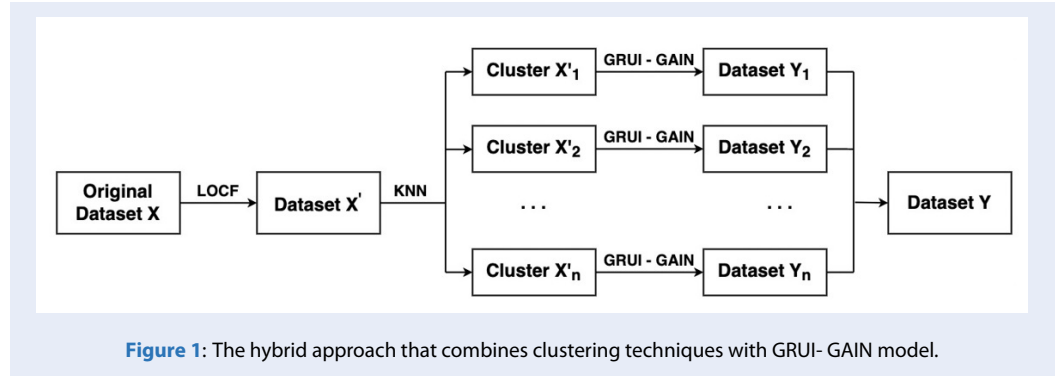


Figure 1: The hybrid approach that combines clustering techniques with GRUI- GAIN model.

229 **B. The Review of GAIN**

230 In the GAIN framework¹⁴, the central components
 231 include the generator G and the discriminator D. An
 232 additional element, known as the hint H, plays a crucial
 233 role.

234 The generator, G, operates by observing a real data
 235 vector, which may contain missing values. It focuses
 236 on imputing these missing values while considering
 237 the information available in the observed data. Ultimately,
 238 it produces a completed vector as its output. The discriminator,
 239 D, takes this completed vector as input and is tasked with
 240 distinguishing between the components of the vector that were
 241 originally observed and those that have been imputed. The
 242 discriminator's role is to assess the authenticity of the imputed
 243 data. Importantly, the hint, H, plays a vital role in this process.
 244 It provides additional information to the discriminator regarding
 245 the missingness of the original sample. Essentially, the hint
 246 ensures that the generator, G, imputes the missing data in a
 247 manner consistent with the true underlying data distribution.

251 In particular, the output of the generator G and discriminator
 252 D in the GAIN framework can be represented as follows:
 253

$$\begin{aligned}
 x_G &= G(X, M, (1 - M) \odot Z) \\
 m_D &= D(z_R, H) \\
 x_R &= M \odot x + (1 - M) \odot x_G
 \end{aligned}$$

254 where Z is a d-dimensional noise and x_R is the reconstructed
 255 sample.

The objectives of GAIN are structured as follows:

$$\begin{aligned}
 &\min_D \frac{1}{N} \sum_{k=1}^N L_D(M, m_D) \\
 &\min_G \frac{1}{N} \sum_{k=1}^N L_D(M, m_D) + \alpha L_R(X, x_R)
 \end{aligned}$$

where α is a weight parameter, L_D, L_G are a cross entropy
 257 loss and L_R is a reconstruction loss. 258

259 **C. GRUI Cell for Generator**

260 We have adopted the GRUI (GRU for Imputation),
 261 proposed in¹², to process the incomplete time series
 262 in the Generator G of GAIN. The GRUI is inspired by
 263 the GRUD⁹. Nevertheless, the GRUI is more simple
 264 than the GRUD. As Figure 2 illustrates, it follows the
 265 structure of GRUD with the removal of the input decay.
 266

267 The key concept behind GRUI is the incorporation
 268 of a time decay vector β , which serves to reduce the
 269 memory retention of the GRU cell. The update functions
 270 of GRUI are outlined below.

$$\begin{aligned}
 \beta_{t_i} &= 1/e^{(0, W_\beta \delta_{t_i} + b_\beta)}, h'_{t_{i-1}} = \beta_{t_i} \odot h_{t_{i-1}} \\
 \mu_{t_i} &= \sigma(W_\mu [h'_{t_{i-1}}, x_{t_i}] + b_\mu) \\
 r_{t_i} &= \sigma(W_r [h'_{t_{i-1}}, x_{t_i}] + b_r) \\
 \tilde{h}_{t_i} &= \tanh(W_{\tilde{h}} [r_{t_i} \odot h'_{t_{i-1}}, x_{t_i}] + b_{\tilde{h}}) \\
 h_{t_i} &= (1 - \mu_{t_i}) \odot h'_{t_{i-1}} + \mu_{t_i} \odot \tilde{h}_{t_i}
 \end{aligned}$$

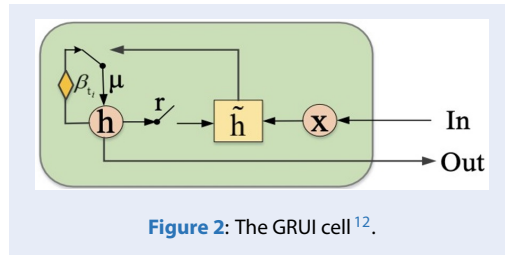


Figure 2: The GRU cell¹².

where δ is the time lag matrix introduced in the “Problem Formulation” part, and $W_\beta, W_r, W_\mu, b_\beta, b_\mu, b_r, b_{\tilde{h}}$ are training parameters. The formulation of β guarantees that with the increase of time lags σ , the value of β decreases. The smaller the σ , the bigger the β . This formulation also makes sure that $\beta \in (0,1]$. While the primary focus of this paper does not revolve around the GRU, it is worth mentioning that our research successfully leverages the GRU within Generator G to effectively process incomplete time series.

The very first input of G is the random noise vector z (random values from a continuous uniform distribution, a common configuration is to use the interval $[-0.01, +0.01]$) and every row of the σ of the fake sample is a constant value. For any incomplete time series x , we try to find the best vector z so that the generated sample x_G is most similar to z . Same as GRU, we add a squared error loss to the loss function of the generator.

D. Discriminator Network Architecture

In contrast to the architecture of GAIN, in our method there is no Hint Generator and, consequently, no Hint Matrix is generated. So, the output of the Discriminator, D, is $m_D = D(x_D)$. Moreover, our Discriminator network adopts a slimmer architecture, consisting of only two layers, in contrast to GAIN’s three-layered Discriminator.

Notably, the Discriminator D in the GRUI-GAIN model adopts the hyperbolic tangent activation function (\tanh) in its output layers. This choice is motivated by two key reasons: firstly, the optimizer used in neural networks tends to converge faster when inputs are linearly transformed to have zero means, unit variances, and are decorrelated, as discussed in the study by LeCun et al.²⁶; secondly, the \tanh activation function’s derivatives are larger than those of the sigmoid, leading to faster convergence for the optimizer when \tanh is employed.

Furthermore, the GRUI-GAIN architecture involves dual Discriminators, one for real data and the other

for fake data. This setup allows for a more comprehensive evaluation and comparison, ensuring the effectiveness of our imputation strategy.

EXPERIMENTAL RESULTS

A. Dataset

For our experimental dataset, we utilize the public bus GPS dataset in India²⁷. As shown in Figure 4, this dataset was obtained from 6 volunteers who were instructed to travel within the sub-urban city of Durgapur, specifically along the route known as “54 Feet.” During their trips on intra-city buses, the volunteers recorded sensor logs using an Android application installed on commercially available smartphones. In this dataset, each round trip covered a total of 24km, and the total distance covered during this entire period is 720km. Following data processing, we selected 102 bus trajectories from the following date ranges: June 26 to July 06, 2019; September 03 to September 05, 2019; and September 12 to September 23, 2019. Table 2 presents a sample of GPS trajectory data from a bus journey on July 3, 2019, where GPS coordinates were recorded at 15-second intervals. Notably, the GPS coordinates were recorded at regular 15-second intervals.

Besides the spatial diversities like populous zones, and marketplaces, ... they also captured data across different timezones starting from 6 AM to 9 PM, each day. For this, they planned the data collection in different time intervals like – 6 AM to 9 AM – Early Morning, 9 AM to 1 PM – Morning, 1 PM to 5 PM – Afternoon, and 5 PM to 9 PM – Evening. Figure 5 illustrates the general data distribution across various time zones.

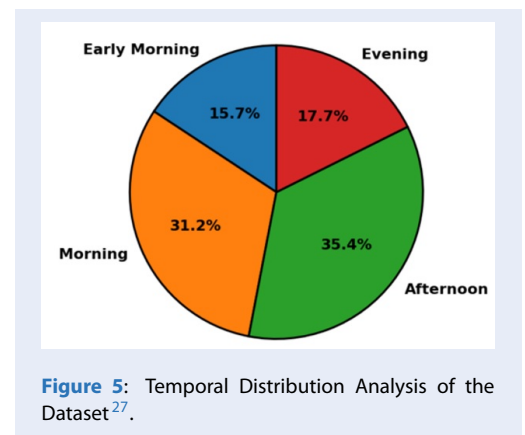


Figure 5: Temporal Distribution Analysis of the Dataset²⁷.

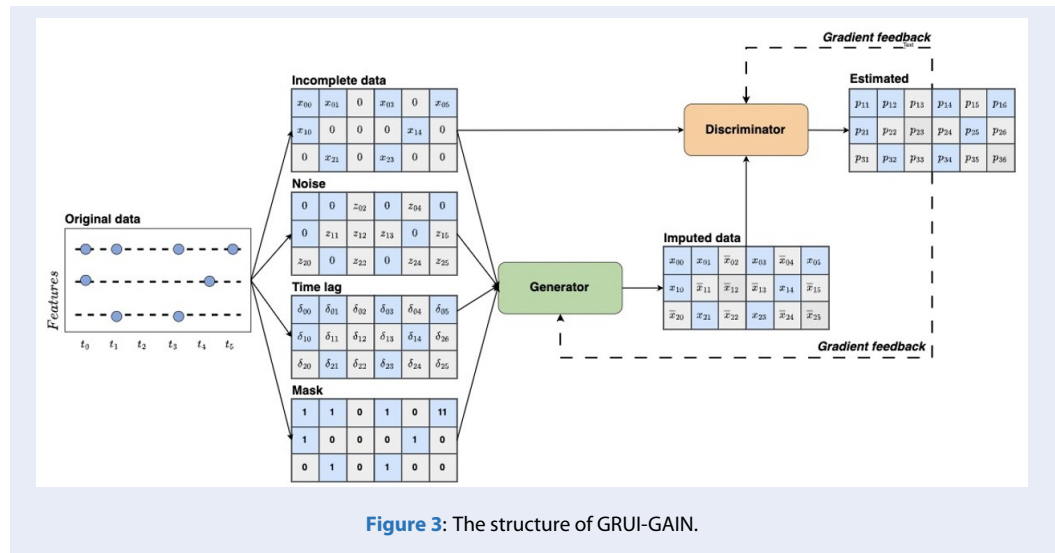


Table 2: GPS Trajectory Data for a Bus Journey on July 3, 2019.

date	timestamp	latitude	longitude
2019-07-03	08:02:20	23.49456677	87.31685814
2019-07-03	08:02:35	23.49458654	87.31684882
2019-07-03	08:02:50	23.49445208	87.31695798
2019-07-03	08:03:05	23.49437571	87.31721719
...
2019-07-03	08:44:20	23.56413802	87.28326889

344 **B. Compared Methods and Performance Indicator**
 345 **ator**

346 In this study, we compare Cluster-GRUI-GAIN with
 347 a range of baseline methods, including:

- 348 • **Mean:** Missing values are replaced with the
 349 mean value of the available data⁴.
- 350 • **Last observed value (LOCF):** Missing values
 351 are replaced with the most recent observed
 352 value²⁵.
- 353 • **K – nearest neighbor (KNN):** Missing values
 354 are imputed by using the values of the k nearest
 355 neighboring samples⁷.
- 356 • **Multivariate Imputation by Chained Equa-
 357 tions (MICE):** Missing values are imputed using
 358 an iterative regression model that estimates the
 359 missing values based on the observed values of
 360 other variables⁶.
- 361 • **GAIN:** GAN-based imputation method that
 362 utilizes a hint vector to impute missing values¹⁴.
- 363 • **E2GAN:** Another GAN-based approach that
 364 employs an auto-encoder structure based on
 365 GRUI as the generator for imputation²¹.

366 These baseline models serve as comparative ap-
 367 proaches for evaluating the performance of the pro-
 368 posed hybrid imputation approach. By contrast-
 369 ing our hybrid approach with these established ap-
 370 proaches, we can assess its effectiveness and advan-
 371 tages in handling missing values in the dataset.
 372 Regardless of the specific imputation technique em-
 373 ployed, the primary objective is to ensure that the im-
 374 puted values closely approximate the true values. To
 375 evaluate the performance of our imputation approach
 376 in our experimental setup, we adopt the Root Mean
 377 Square Error (RMSE) as our metric. A smaller RMSE
 378 indicates superior results, highlighting the accuracy
 379 and effectiveness of the imputation process. By mini-
 380 mizing the RMSE, we aim to achieve the highest level
 381 of fidelity between the imputed values and the ob-
 382 served value.

$$RMSE = \sqrt{\frac{\sum_{n=1}^N (X_{obs} - Y_{imp})^2}{N}}$$

383 where x_{obs} is the observed value, Y_{imp} is the imputed
 384 value.

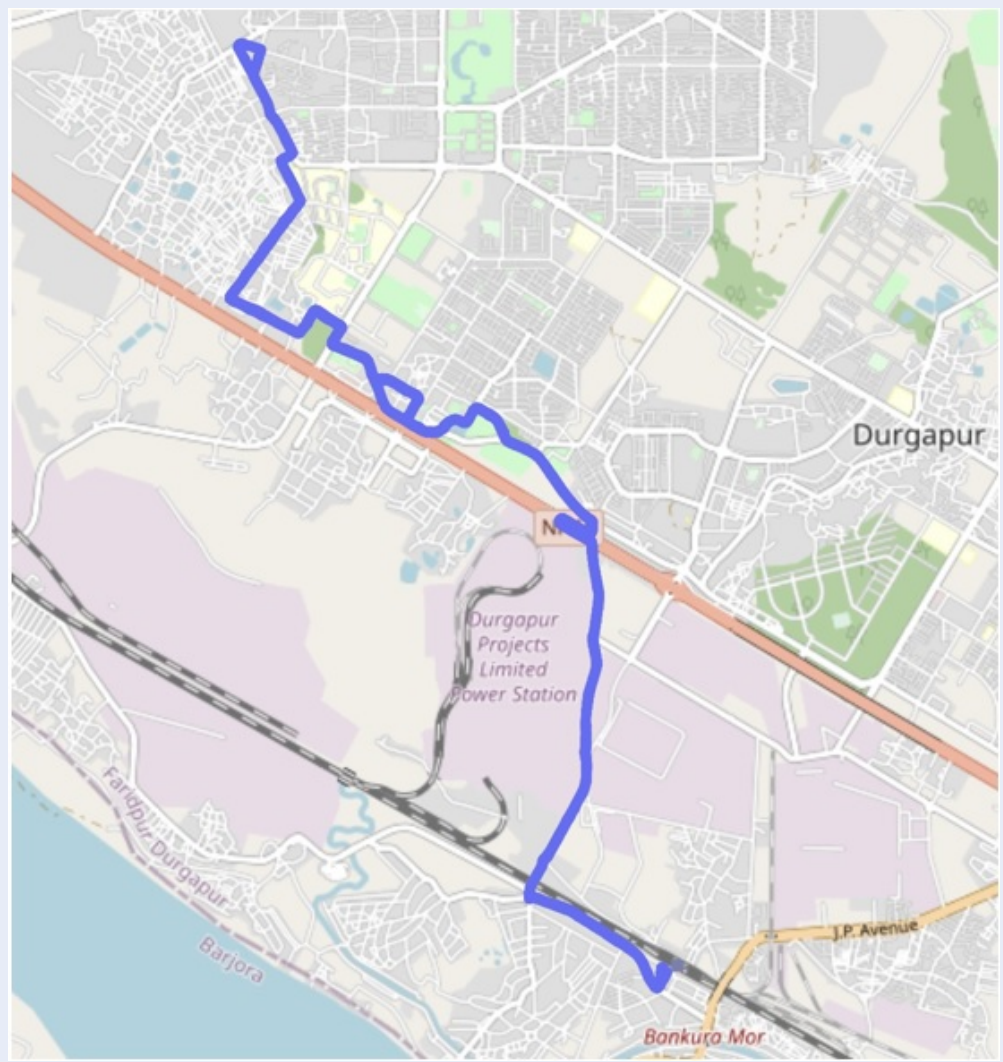


Figure 4: The GPS bus trajectory dataset utilized in this study was collected from the suburban city of Durgapur, located in India.

385 **C. Details of Implementation**

386 In our study using the dataset from²⁷, we systemati-
 387 cally evaluate missing data imputation by randomly
 388 dropping between 10% and 80% of trajectory data.
 389 We then impute these missing values and assess ac-
 390 curacy using RMSE.

391 The GRUI cells employ 16 hidden units, a fixed 0.3
 392 dropout rate, and incorporate batch normalization.
 393 We standardize input data to have zero mean and unit
 394 variance. We allocate 15% of the dataset each for val-
 395 idation and testing. Key parameters for this dataset
 396 include an epoch of 10, a batch size of 16, a learning
 397 rate of 0.002, and λ set to 2 for regularization.

398 **D. Performance Comparison for GPS Trajec- 399**
tory Data

400 In Table 3, we present the RMSE results of the pro-
 401 posed hybrid approach and the baseline models. The
 402 missing rate, indicating the percentage of dropped
 403 values, is listed in the first column, while the subse-
 404 quent columns display the corresponding RMSE val-
 405 ues. Notably, the GAN-based methods consistently
 406 exhibit the highest imputation accuracies across all
 407 scenarios. The proposed hybrid approach, Cluster-
 408 GRUI-GAIN, emerges as one of the top-performing
 409 methods, outperforming other approaches in most
 410 cases. Additionally, the proposed hybrid approach
 411 demonstrates a significant advantage in handling
 412 large missing gaps, which will be further explored and

413 discussed in the latter part of this paper.

414 **E. Imputation Accuracy Under Clustering**

415 Figure 6 illustrates the trends of RMSE for Cluster-
 416 GRUI-GAIN and the comparison algorithms (GRUI-
 417 GAIN without clustering, GAIN, and KNN) when
 418 imputing GPS trajectory data with varying missing
 419 rates. While both GAIN and GRUI-GAIN are affected
 420 by data sparsity, resulting in fluctuating imputation
 421 performance as the missing rate increases, Cluster-
 422 GRUI-GAIN effectively addresses the data sparsity
 423 challenge under high missing rates. This leads to im-
 424 proved robustness and enhanced accuracy for datasets
 425 with higher missing rates.

426 As a result, the hybrid approach is well-suited for han-
 427 dling datasets with higher missing rates or greater
 428 sparsity in practical applications.

429 Additionally, we investigate the impact of the number
 430 of clusters on the performance of our proposed ap-
 431 proach. Figure 7 illustrates that, across various miss-
 432 ing rates, Cluster-GRUI-GAIN consistently achieves
 433 better results when the number of clusters is set to 3.
 434 This finding holds true for most cases in the dataset,
 435 indicating the robustness and effectiveness of our ap-
 436 proach in terms of imputation performance. Regard-
 437 less of the missing rate, selecting $K=3$ yields favorable
 438 outcomes with our hybrid approach.

439 **DISCUSSION**

440 **Different Gap Size Analysis**

441 In order to assess the imputation accuracy of the
 442 hybrid imputation approach, we examine its perfor-
 443 mance under different gap sizes. Specifically, we ran-
 444 domly remove 15-minute, 30-minute, and 45-minute
 445 of data from random trajectories, creating gappy time
 446 series for analysis. As depicted in Figure 8, we observe
 447 a deterioration in imputation accuracy as the gap size
 448 increases. This decline can be attributed to the dimi-
 449 nishing temporal correlation as the gap size expands.

450 However, the hybrid imputation approach, which
 451 leverages the clustering method to generate a repre-
 452 sentative training dataset, exhibits superior modeling
 453 capabilities compared to E2GAN. Consequently, the
 454 hybrid imputation approach is more suitable for han-
 455 dling datasets with a higher missing gap in practical
 456 applications.

457 **CONCLUSIONS AND FUTURE WORK**

458 In conclusion, this research introduces Cluster-
 459 GRUI-GAIN, a novel hybrid imputation approach de-
 460 signed to enhance the accuracy of imputing time se-
 461 ries data, particularly GPS trajectory data. By com-
 462 bining clustering techniques with the improved gen-
 463 erative adversarial imputation network, GRUI-GAIN,

our approach addresses the challenge of missing data 464
 in transportation systems. Our extensive experiments 465
 on real-world datasets have demonstrated the supe- 466
 riority of Cluster-GRUI-GAIN over baseline meth- 467
 ods. It consistently achieves higher imputation accu- 468
 racy, making it especially well-suited for datasets with 469
 higher missing rates and significant gaps. Further- 470
 more, our approach exhibits resilience when faced 471
 with data sparsity and outperforms other methods in 472
 handling large missing gaps. This research signifies 473
 a significant step forward in the field of data impu- 474
 tation for transportation systems, with the potential 475
 to impact various practical applications in the real 476
 world. Future work will explore broader applications 477
 and fine-tune clustering parameters to further opti- 478
 mize the approach. 479

This study highlights the potential of combining clus- 480
 tering and deep generative models to tackle complex 481
 data imputation tasks. In future research endeavors, 482
 we aspire to extend the utility of our hybrid impu- 483
 tation approach to diverse domains beyond GPS 484
 trajectories. Our objectives include exploring varied 485
 clustering methodologies and conducting perfor- 486
 mance evaluations on an even wider array of real- 487
 world datasets. Additionally, we plan to perform 488
 comprehensive experimental comparisons, including 489
 benchmarking against state-of-the-art methods such 490
 as SSGAN²², in the context of multivariate time series 491
 data imputation within the GPS trajectory domain. 492

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 HCM. 499

500 **CONFLICT OF INTEREST**

The authors declare that they have no competing in- 501
 terests. 502

503 **AUTHOR CONTRIBUTION**

Nam Thoai, Nguyen Tran Tho, Trung Dang Anh and 504
 Thanh Hoang Le Hai provided guidance and strategic 505
 direction and shaping research objectives. 506

Khang Nguyen Duy made sub-stantial contributions 507
 by actively engaging in data collection, model devel- 508
 opment, experimental work, and constructive discus- 509
 sions. 510



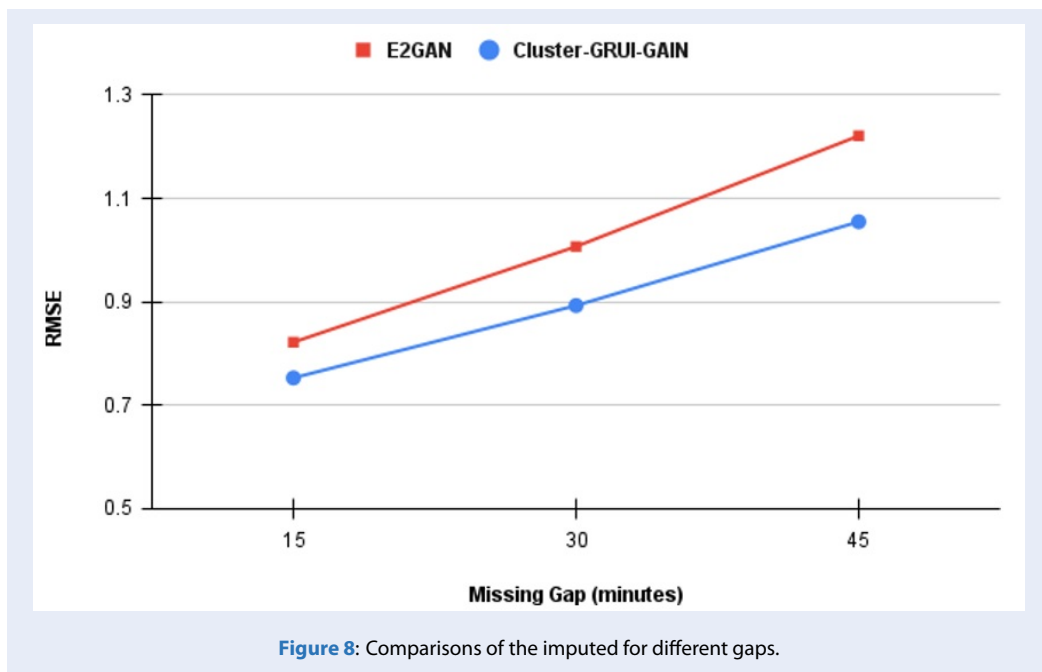
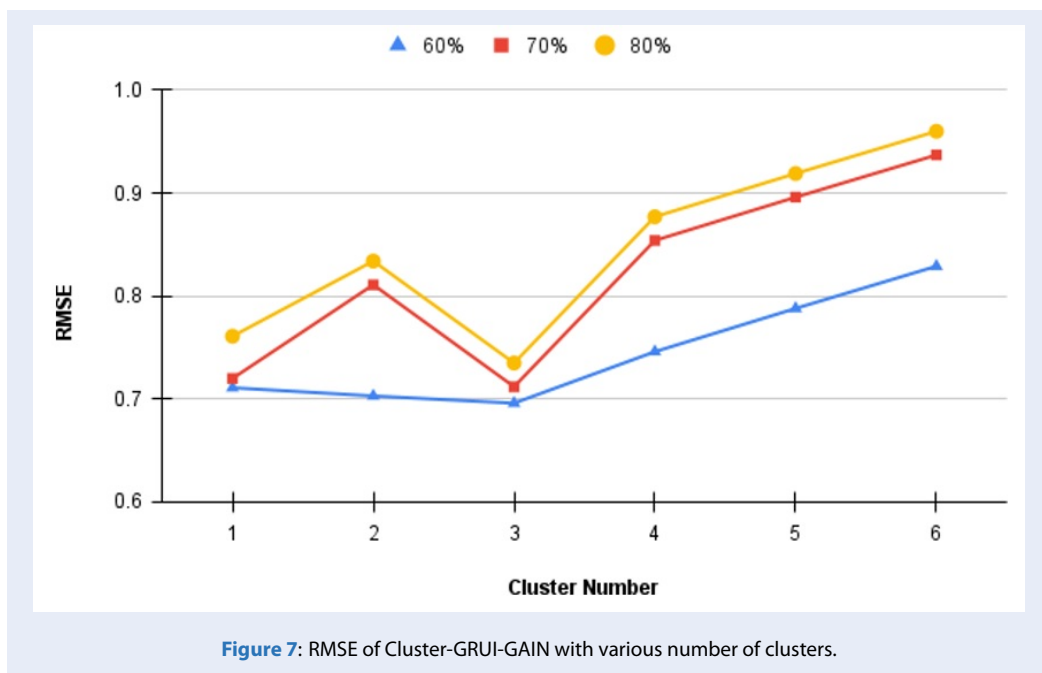
Figure 6: Imputation accuracy under clustering.

Table 3: The RMSE (the smaller, the better) results of Cluster-GRUI-GAIN and other baseline imputation methods on the GPS bus trajectory dataset.

Missing Rate (%)	Mean ⁴	LOCF ²⁵	KNN ⁷	MICE ⁶	GAIN ¹⁴	E2GAN ²¹	Cluster-GRUI-GAIN
10	0.846	0.366	0.548	0.554	0.374	0.286	0.307
20	0.804	0.538	0.610	0.548	0.516	0.448	0.466
30	0.991	0.721	0.647	0.691	0.637	0.572	0.579
40	0.940	0.676	0.694	0.680	0.652	0.626	0.624
50	0.866	0.724	0.736	0.744	0.676	0.609	0.604
60	0.892	0.747	0.778	0.758	0.742	0.709	0.696
70	0.988	0.858	0.784	0.868	0.762	0.716	0.712
80	1.075	0.863	0.857	1.047	0.805	0.748	0.735

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Bổ khuyết lộ trình di chuyển GPS: Phương pháp tiếp cận kết hợp thuật toán phân cụm và giải thuật dựa trên GAIN

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TÓM TẮT

Với Sự tiến bộ về sức mạnh tính toán và sự phát triển của dữ liệu lớn đã mở ra những cơ hội chưa từng có cho cộng đồng Hệ thống Giao thông Thông minh (ITS) để trích xuất những thông tin quý giá từ dữ liệu quỹ đạo dữ liệu quỹ đạo Hệ thống Định vị Toàn cầu (GPS). Tuy nhiên, thực tế của dữ liệu quỹ đạo GPS trong thế giới thực thường thiếu thông tin đầy đủ do nhiều yếu tố khác nhau (ví dụ: hồng cảm biến, mất truyền, ...), từ đó đặt ra những thách thức đáng kể cho việc phân tích quỹ đạo và hiệu quả hoạt động trong các hệ thống giao thông. Để giải quyết vấn đề này, các kỹ thuật bổ khuyết dữ liệu chuỗi thời gian đã xuất hiện như những giải pháp quan trọng để điền vào các điểm dữ liệu bị thiếu một cách chính xác. Các phương pháp bổ khuyết hiện có có thể được phân loại thành các phương pháp thống kê và mô hình tạo sinh sâu. Đáng chú ý, trong lĩnh vực của các mô hình tạo sinh sâu, Mạng Bổ Khuyết Đối Nghịch Tạo Sinh Dữ Liệu (GAIN) đã thể hiện tiềm năng trong lĩnh vực bổ khuyết dữ liệu. Tuy nhiên, khả năng hạn chế của chúng trong việc xử lý hiệu quả dữ liệu chuỗi thời gian là một hạn chế đáng chú ý. Ngoài ra, các quỹ đạo GPS, đặc biệt là của các xe buýt, có đặc điểm độc đáo khi mỗi phương tiện được gán vào một hoặc nhiều tuyến đường đã được xác định trước, tạo ra sự phức tạp trong quá trình bổ khuyết dữ liệu.

Để đáp ứng những thách thức này, nghiên cứu này đề xuất một phương pháp bổ khuyết kết hợp mới, Cluster-GRUI-GAIN, kết hợp các kỹ thuật phân cụm (ví dụ: KNN) với mạng bổ khuyết đối nghịch tạo sinh được cải thiện, GRUI-GAIN. Bằng cách kết hợp những ưu điểm của phân cụm và GAIN, phương pháp kết hợp của chúng tôi nhằm mục tiêu nâng cao độ chính xác của việc bổ khuyết dữ liệu chuỗi thời gian cho các quỹ đạo GPS với các tỷ lệ thiếu khác nhau và các khoảng trống đáng kể. Cụ thể, mô hình GRUI-GAIN trong Cluster-GRUI-GAIN mà chúng tôi đề xuất tích hợp GRUI (GRU cho Imputation) vào bộ tạo sinh. Sự tích hợp chiến lược này cải thiện khả năng của mô hình trong việc xử lý dữ liệu thiếu trong chuỗi thời gian, từ đó tăng cường độ chính xác và đáng tin cậy của các giá trị bổ khuyết. Đánh giá thực nghiệm trên bộ dữ liệu thế giới thực cho thấy rằng phương pháp Cluster-GRUI-GAIN mà chúng tôi đề xuất vượt qua các phương pháp cơ sở về độ chính xác của việc bổ khuyết dữ liệu chuỗi thời gian và cung cấp các bổ khuyết mạnh mẽ và chính xác, làm cho nó phù hợp cho các ứng dụng.

Từ khóa: lộ trình GPS, bổ khuyết dữ liệu, mạng đối nghịch tạo sinh, gom cụm, kết hợp

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